Using the SCDA package (0.8) for analysing single and multiple case AB designs

Jürgen Wilbert, University Potsdam

Content

Prerequisites	2
Introduction and an example	2
Descriptives	8
Percent non-overlapping data	9
Percent exceeding the median	9
Percent all non-overlapping data	10
Non-overlap of all Pairs	11
Percent exceeding the trend	12
Reliable Change Index	13
Linear trends	14
Piecewise linear model	15
Randomization tests	17
Plot AB-designs	18
Smoothing	21
Outlier	22
Fill in missing measurement times	2 3
Importing and exporting data	24
Selecting data	25
Random sample generator	25
Aggregate multiple cases into one case	28
*(Experimental) Power Analysis	29
Reference	31

This document gives an introduction to the SCDA (single-case data analysis) R-package. The current version can be reached via

http://tinyurl.com/SCDA-Manual

The SCDA package was designed for analysing and visualizing single-case AB data sets. These designs are commonly used for evaluating learning progress and curriculum-based measurements. Furthermore, the SCDA package comprises a module for generating random single and multiple-baseline datasets under a variety of circumstances for conducting Monte-Carlo studies on the power of single-case analysing techniques.

Prerequisites

Firstly, you have to install the R statistical program. Therefore, go to the R homepage (http://www.r-project.org) and choose the appropriate download file for your system.

The SCDA package is currently stored in a single R file and can be accessed via the internet at http://tinyurl.com/SCDA-for-R. You can implement and activate it into your R system using the source command:

```
source("http://tinyurl.com/SCDA-for-R")
```

You can reach a developmental version under (which is only recommended if you encounter an error):

```
source("http://tinyurl.com/SCDA-develop")
```

Introduction and an example

The SCDA package offers several methods for coding single-case data. The simplest way is to use a vector of values, each representing one measurement.

In R, a vector is built in the following way:

```
y \leftarrow c(5, 7, 8, 5, 7, 12, 16, 18, 15, 14, 19)
```

y is the name of the variable. A chain of 11 values is ascribed to it by the arrow operator (<-). You can control the ascription by typing in the name of the variable and get the following result:

```
> y
[1] 5 7 8 5 7 12 16 18 15 14 19
```

For a graphical output of y, use the plotSC command. The parameter B. start informs the function about the start of the B-phase.

```
plotSC(y, B.start = 6)
```

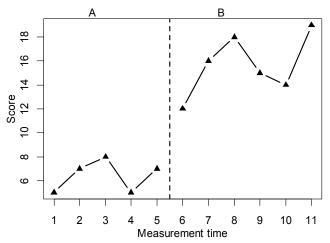


Figure. Simple plot

For a first overview, use the describesc command:

> describeSC(y, B.start = 6)
Describe single-case data

	Person1	total
n A	5.00	5.00
n B	6.00	6.00
Mean A	6.40	6.40
Mean B	15.67	15.67
Mean dif	9.27	9.27
SD A	1.34	1.34
SD B	2.58	2.58
SD AB	5.24	5.24
SMD A	6.91	6.91
SMD B	3.59	3.59
SMD AB	1.77	1.77
Autocor A	-0.41	-0.41
Autocor B	-0.19	-0.19
Trend A	0.20	0.20
Trend B	0.74	0.74
Trend AB	1.40	1.40
PND	100.00	100.00
PEM	100.00	100.00
NAP	100.00	100.00
PAND	100.00	100.00

While this way of coding the data is handy and applicable to all functions in the SCDA package, the SCDA package internally uses a list of data frames to process single-case data. This allows for a higher flexibility in processing and portability of the data. A data frame is a spreadsheet like object to store data of different variables for a number of cases. The data frame for the above used example is:

phase	values	mt
A	5	1
A	7	2
A	8	3
A	5	4
A	7	5
В	12	6
В	16	7
В	18	8
В	15	9
В	14	10
В	19	11

The first column contains the phase of the measurement, the second the measured values, and the third the measurement times. To create a data frame object you type in:

```
person1 <- makeSCDF(c(5, 7, 8, 5, 7, 12, 16, 18, 15, 14, 19), B.start = 6)
```

If the MT variable is left out, it is internally built with values from 1...n (n is the number of measurements). The commands plotSC(person1) and describeSC(person1) would give the same results as before.

Alternatively, we can type the data into an external spreadsheet program like EXCEL or CALC, save them as a CSV file (comma-separated values), and load them into R:

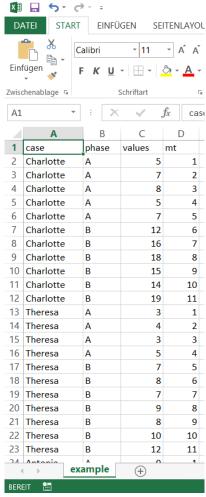


Figure. Using EXCEL to create and data frame for one or multiple single cases.

```
person1 <- readSC(file.choose())</pre>
```

if you set up your computer system in a European country it may be necessary to use

```
person1 <- readSC(file.choose(), sep = ";", dec = ",")</pre>
```

instead, as the spreadsheet program writes semicolon separated files and a comma as a decimal sign using the CSV output format. Note that the spreadsheet you want to import must have variable names in the first row and the names of the cases in the first column. The first column is necessary even if you have only one case.

As a third alternative, we can use the built in data editor of R:

person1 <- edit(data.frame())</pre>

R	D	ateneditor	_ 🗆 ×
Datei	Bearbeiten H	ilfe	
	phase	value	mt
1	A	2	1
2	A	2	2
3	A	4	3
4	A	6	4
5	A	7	5
6	В	12	6
7	В	13	7
8	В	14	8
9	В	15	9
10	В	16	10
11			
12			
13			

Figure: R's built in data editor.

Consider the case we have a multiple-baseline dataset of three persons. We may code these in the following way:

```
charlotte <- makeSCDF(c(5, 7, 8, 5, 7, 12, 16, 18, 15, 14, 19), 6) theresa <- makeSCDF(c(3, 4, 3, 5, 7, 8, 7, 9, 8, 10, 12),5) antonia <- makeSCDF(c(9, 8, 8, 7, 5, 7, 13, 14, 15, 12, 16), 7) study1 <- list(charlotte, theresa, antonia) names(study1) <- c("Charlotte", "Theresa", "Antonia")
```

Firstly, we define three data frames. Then we combine the three data frames into a list with the name study1. For a nicer look, we added the optional names function to give each case an appropriate name that will be used subsequently in different SCDA functions (note that the name of the parameter B.start can be left out here because the value is placed exactly at the second position).

Now we can use the plotsc command to draw a graphic. To oversee the percent non-overlapping data we added a line representing the maximum of the A-phase using the lines = "maxA" parameter:

```
plotSC(study1, lines = "maxA")
```

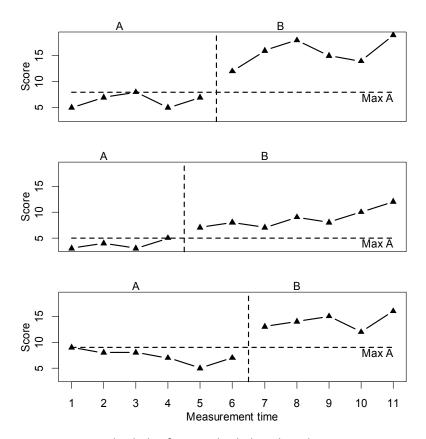


Figure. SCDA standard plot for a multiple baseline design.

We get an overview of the data with the describesc command.

> describeSC(study1)
Describe single-case data

	charlotte	theresa	antonia	total	total(makesingleSC)
n A	5.00	4.00	6.00	15.00	15.00
n B	6.00	7.00	5.00	18.00	18.00
n AB	11.00	11.00	11.00	33.00	33.00
Missing A	0.00	0.00	0.00	0.00	0.00
Missing B	0.00	0.00	0.00	0.00	0.00
Missing AB	0.00	0.00	0.00	0.00	0.00
Mean A	6.40	3.75	7.33	5.83	0.00
Mean B	15.67	8.71	14.00	12.79	6.87
Mean dif	9.27	4.96	6.67	6.97	6.87
Min A	5.00	3.00	5.00	3.00	-2.33
Min B	12.00	7.00	12.00	7.00	3.25
Max A	8.00	5.00	9.00	9.00	1.67
Max B	19.00	12.00	16.00	19.00	12.60
SD A	1.34	0.96	1.37	1.24	1.17
SD B	2.58	1.80	1.58	2.03	2.69
SD AB	5.24	2.91	3.75	4.08	4.06
SMD A	6.91	5.19	4.88	5.66	5.85
SMD B	3.59	2.76	4.22	3.52	2.56
SMD AB	1.77	1.70	1.78	1.75	1.69
Autocor A	-0.41	-0.48	0.31	-0.19	-0.18
Autocor B	-0.19	0.26	-0.60	-0.18	-0.18
Trend A	0.20	0.50	-0.57	0.04	-0.16
Trend B	0.74	0.71	0.40	0.62	0.53
Trend AB	1.40	0.84	0.85	1.03	0.89
Trend dif	0.54	0.21	0.97	0.58	0.69
PND	100.00	100.00	100.00	100.00	100.00

```
    PEM
    100.00
    100.00
    100.00
    100.00

    NAP
    100.00
    100.00
    100.00
    100.00

    PAND
    100.00
    100.00
    100.00
    100.00
```

For analysing the example, we compute the percent all non-overlapping data (Parker, Hagan-Burke, & Vannest, 2007) by the pand command.

```
Percent all non-overlapping data
PAND = 100 %
Phi = 1 ; Phi-square = 1
Number of persons: 3
Total measurements: 33
in phase A: 15
in phase B: 18
n Overlapping data per person: 0, 0, 0
n Overlapping data: 0
% Overlapping data: 0
2 x 2 Matrix
       % expected
       Α
            В
                       total
   A 45
               0
                       45
real B 0
               55
                       55
total 45
               55
Note. Matrix is corrected for ties (Wilbert, 2013)
Then we conduct a multiple-baseline randomization test:
> set.seed(1234) #only needed for replicating the following results exactly
> rand.test(study1, limit = 4, complete = TRUE)
Randomization test
Multiple-Baseline test for 3 cases.
Statistic: Mean B-A
Length A-phase 15
Length B-phase 18
Minimal length of phase: 4
```

```
Based on all 64 possible combinations.
```

Observed statistic = 6.965873

```
Distribution:
n = 64
M = 6.215873
SD = 0.428785
Min = 5.280952
Max = 6.965873
p = 0.015625
```

> pand(study1)

```
Shapiro-Wilk normality test: W = 0.965; p = 0.065 (hypothesis of normality maintained) z = 1.7491, p = 0.0401 (single sided)
```

Moreover, as a parametric approach, we compute a piecewise-linear-regression model (Beretvas & Chung, 2008; Huitema & Mckean, 2000):

```
> plm(study1)
Piecewise Regression Analysis
Multiple Baseline Design for 3 cases.
Regression model: B&L-B
F(3, 29) = 31.20; p = 0.000; R-Square = 0.763; adjusted R-Square = 0.739
                                 p R-Square
               В
                    SE
                            t
Intercept 0.483 1.203 0.401 0.691
Trend -0.157 0.351 -0.448 0.657
                                        0.002
          5.457 1.588 3.437 0.002
0.685 0.444 1.543 0.134
Level
                                        0.096
                                        0.019
Slope
```

All analyses suggest that the values in the B-phase of the study are higher than in the A-phase.

After this session, we save the data with the standard R procedure <code>save()</code> into a file.

```
save(study1, file = "study1.RData")
```

If you have problems finding the right folder on your hard disk, you can choose the file.choose() command instead of the file name.

```
save(study1, file = file.choose())
```

Later you can load the data with the load command.

```
load("study1.RData") Or load(file.choose())
```

Alternatively, you can export the data into a CSV file with writesc and later read them again with readSC.

```
writeSC(study1, "study1.csv")
study1 <- readSC("study1.csv")</pre>
```

If you have chosen the right delimiter and decimal separator, you can open the study1.csv file into your spreadsheet program by a double-click.

Descriptives

Description

The describesc command gives some important descriptives of your single-case data including trends, standardized mean differences, measurements for data overlap, and autocorrelation.

Example

```
set.seed(1234)
dat <- rSC(5, B.start = c("rand", 5, 10), d.level = 1.0, d.slope = 0.1, trend =
0.05, rtt = 0.75, round = 0, random.names = TRUE)
describeSC(dat)</pre>
```

Describe single-case data

```
Bradyn August Krish Antoine Mckayla total total (makesingleSC)
                     7.00 7.00 8.00 34.00
         5.00 7.00
         15.00 13.00 13.00 13.00 12.00 66.00
                                                       66.00
nВ
         20.00 20.00 20.00 20.00 20.00 100.00
n AB
                                                      100.00
Missing A 0.00 0.00 0.00 0.00
                                 0.00 0.00
                                                        0.00
Missing B 0.00 0.00 0.00 0.00 0.00 0.00
                                                        0.00
Missing AB 0.00 0.00 0.00 0.00 0.00 0.00
                                                        0.00
Mean A
        56.40 42.71 61.57 68.29 53.50 56.49
                                                         0.00
```

Mean B	76.67	62.00	85.62	86.08	78.42	77.76	21.18
Mean dif	20.27	19.29	24.04	17.79	24.92	21.26	21.18
Min A	49.00	35.00	53.00	63.00	41.00	35.00	-12.50
Min B	61.00	51.00	69.00	72.00	71.00	51.00	3.71
Max A	63.00	52.00	68.00	79.00	69.00	79.00	15.50
Max B	89.00	78.00	98.00	98.00	90.00	98.00	36.50
SD A	5.64	5.71	5.38	5.59	9.37	6.52	6.27
SD B	10.15	8.74	10.44	8.48	7.19	9.08	9.26
SD AB	12.79	12.15	14.71	11.45	14.80	13.25	13.08
SMD A	3.59	3.38	4.47	3.18	2.66	3.46	3.38
SMD B	2.00	2.21	2.30	2.10	3.46	2.41	2.29
SMD AB	1.58	1.59	1.63	1.55	1.68	1.61	1.62
Autocor A	0.33	-0.44	-0.37	0.28	0.58	0.08	0.31
Autocor B	0.56	0.63	0.62	0.75	0.33	0.58	0.51
Trend A	3.30	1.29	1.00	1.11	2.88	1.91	1.74
Trend B	1.96	1.88	2.25	1.98	1.59	1.93	1.88
Trend AB	2.02	1.89	2.30	1.81	2.32	2.07	1.89
Trend dif	-1.34	0.59	1.25	0.88	-1.29	0.02	0.14
PND	86.67	84.62	100.00	76.92	100.00	89.64	69.70
PEM	100.00	100.00	100.00	100.00	100.00	100.00	100.00
NAP	97.33	97.80	100.00	96.70	100.00	98.37	97.42
PAND	90.00	85.00	100.00	90.00	100.00	93.00	92.00

Parameters and Arguments

data, B. start and MT: Specification of the data. Read the "Introduction and example" chapter for a description.

decreasing: If you expect the data to be lower in the B phase, set decreasing = TRUE (default is FALSE).

Percent non-overlapping data

Description

The function pnd return the percentage non-overlapping data. If you expect a decrease in the B-phase, set the parameter decreasing = TRUE. Due to its error-proneness you should not use PND but NAP or PAND instead (see Parker & Vannest, 2009).

Parameters and Arguments

data, B. start and MT: Specification of the data. Read the "Introduction and example" chapter for a description.

decreasing: If you expect the data to be lower in the B phase, set decreasing = TRUE (default is FALSE).

Percent exceeding the median

Description

The function pem return the percentage of the B-phase data exceeding the median of the A-phase data. Additionally, a X^2 test against a 50/50 distribution is computed. Different measures of central tendency could be addressed for alternative analyses. If you expect a decrease in the B-phase, set the parameter decreasing = TRUE.

Parameters and Arguments

 $\mathtt{data}, \mathtt{B.start}$ and $\mathtt{MT}:$ Specification of the data. Read the "Introduction and example" chapter for a description.

decreasing: If you expect the data to be lower in the B phase, set decreasing = TRUE (default is FALSE).

binom.test: Computes a binomial test for a 50/50 distribution. By default set TRUE.

chi.test: By default set FALSE. If set FALSE the Chi² Test is skipped.

FUN: By default median. Alternatively, you could implement any other function for computing an average.

...: Additional arguments for the FUN parameter (e.g. FUN = mean, trim = 0.1 will use a 10% trimmed mean instead of a median for analysing the data).

Example

```
set.seed(1234)
dat <- rSC(5, d.level = 0.5)
pem(dat)

Percent Exceeding the Median

PEM binom.p Chi DF p

Case 1 60.000 0.304 0.600 1 0.439

Case 2 86.667 0.004 8.067 1 0.005

Case 3 100.000 0.000 15.000 1 0.000

Case 4 20.000 0.996 5.400 1 0.020

Case 5 100.000 0.000 15.000 1 0.000

Alternative hypothesis: true probability > 50%
```

Percent all non-overlapping data

Description

The percent non-overlapping data is a measurement for estimating a level increase (or decrease) in performance after an intervention. It can be computed with the pand command. PAND allows for a Chi² statistical test (comparing real and estimated association a data points with phase A and B) and thereby allows an estimation of the effect size phi, which is identical to Pearsons r computed with dichotomous data. Phi² is thus the amount of explained variance. The original procedure for computing PAND as proposed by Parker and colleagues (Parker u. a., 2007) does not take ambivalent data points due to ties into account, as does the computation for the nonoverlap of all pairs index (Parker & Vannest, 2009). In the pand procedure, the frequency matrix is corrected for ties.

Example

A simple example:

```
> set.seed(1234)
> dat <- rSC(1, d.level = 1.0)
> pand(dat)

Percent all non-overlapping data

PAND = 90 %
Phi = 0.733 ; Phi-square = 0.538

Number of persons: 1
Total measurements: 20
in phase A: 5
in phase B: 15
```

```
n Overlapping data per person: 2
n Overlapping data: 2
% Overlapping data: 10
2 x 2 Matrix
       % expected
          В
                    total
       Δ
            5
    A 20
                     25
             70
real B 5
 total 25
             75
Note. Matrix is corrected for ties (Wilbert, 2013)
```

Computing PAND when expecting a decrease in performance after intervention in a multiple-baseline design:

```
> set.seed(1234)
> dat <- rSC(3, B.start = c(5, 7, 9), d.level = -1.0)
> pand(dat, decreasing = TRUE)
Percent all non-overlapping data
PAND = 80 %
Phi = 0.524 ; Phi-square = 0.274
Number of persons: 3
Total measurements: 60
in phase A: 18
in phase B: 42
n Overlapping data per person: 2, 4, 6
n Overlapping data: 12
% Overlapping data: 20
2 x 2 Matrix
       % expected
       A B 10
                     total
    A 20
                      30
real B 10
             60
                      70
 total 30
              70
```

Note. Matrix is corrected for ties (Wilbert, 2013)

Parameters and Arguments

data, B. start and MT: Specification of the data. Read the "Introduction and example" chapter for a description.

decreasing: If you expect the data to be lower in the B phase, set decreasing = TRUE (default is FALSE).

correction: If set TRUE, a correction for ties conducted (default is TRUE).

Non-overlap of all Pairs

Description

The index Nonoverlapping of all pairs was developed by Parker and colleagues (Parker & Vannest, 2009). It is recommended as an overlapping measurement.

Example

```
> set.seed(1234)
> dat <- rSC(1, d.level = -1.0)
> nap(dat, decreasing = TRUE)
Non-overlap of All Pairs
N persons = 1
NAP = 92 %
Rescaled NAP = 84 %
```

Parameters and Arguments

data, B. start and MT: Specification of the data. Read the "Introduction and example" chapter for a description.

decreasing: If you expect the data to be lower in the B phase, set decreasing = TRUE (default is FALSE).

Percent exceeding the trend

Description

The function pet return the percentage of the B-phase data exceeding the predicted values on basis of the trend of the A-phase. A binomial test against a 50/50 distribution is computed. Furthermore, the percent of data points in the B-phase exceeding the upper (or lower) threshold of the 95% confidence interval of the predicted values is returned. If you expect a decrease in the B-phase, set the parameter decreasing = TRUE.

Parameters and Arguments

data, B. start and MT: Specification of the data. Read the "Introduction and example" chapter for a description.

decreasing: If you expect the data to be lower in the B phase, set decreasing = TRUE (default is

ci: The size of the confidence interval (by default ci = .95).

Example

```
set.seed(1234)
dat \leftarrow rSC(5, d.slope = 0.2)
pet(dat)
Percent Exceeding the Trend
N persons = 5
          PET binom.p PET CI
Case 1 93.333 0.000 0
Case 2 93.333 0.000
                       100
Case 3 100.000
               0.000
Case 4 46.667
               0.696
                       100
               0.000
Case 5 100.000
```

Binom.test: alternative hypothesis: true probability > 50%

PET CI: Percent of values greater than upper 95% confidence threshold (greater 1.645*se above predicted value)

Reliable Change Index

Description

Example

Computes different measures for a reliable change index (see Wise, 2004).

Reliable Change Indices:

RCI
Jacobson et al. 50.62279
Christensen and Mendoza 35.79572
Hageman and Arrindell 17.92417

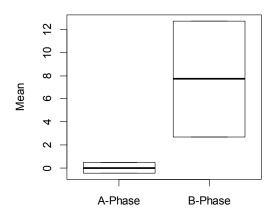
A-Phase -0.08009117 0.8800912 B-Phase 7.86160191 17.7383981

RCI for multiple single-cases with a graph:

Jacobson et al. 32.05714

```
rci(byHeartSC, graph = TRUE)
Reliable Change Index
N persons = 6
Data of cases are aggregated using the makesingleSC command.
Mean difference = 7.715789
Standardized difference = 1.284888
Descriptives:
                  mean
                              SD
A-Phase 30 7.397813e-18 0.5381962 0.2406887
B-Phase 95 7.715789e+00 5.7480120 2.5705891
Reliability = 0.8
95 % confidenzintervals:
            Lower Upper
A-Phase -0.4717411 0.4717411
B-Phase 2.6775274 12.7540515
Reliable Change Indices:
```

95% confidence interval



Parameters and Arguments

data, B. start and MT: Specification of the data. Read the "Introduction and example" chapter for a description.

rel: Reliability necessary for computing standard errors. Default is rel = 0.8.

ci: Span of the confidence interval (default is ci = 0.95 indicating a 95% confidence interval).

graph: If set TRUE, a boxplot with the mean of the A and B-phase and the confidence intervals is plotted (default is FALSE).

Linear trends

Description

If you want to get an overview of linear trends in the different phases of a single-case you can use the trendsc command. By default, it gives you the intercept and slope of a linear and a squared regression model of the measurement-time on the values. Models are computed for the A phase, the B-phase (with correcting the measurement-time to start at one), and the combined A and B-Phase. For a more advanced application, you can add further regression models using the R specific formula class, which will be applied again to the A-phase, the B-phase, and the combined A and B-phase.

Parameters and Arguments

data, B. start and MT: Specification of the data. Read the "Introduction and example" chapter for a description.

B.offset: An offset for the first measurement-time (MT) of the B-phase. If set 0, the first MT of the B-phase is set to 1. The default is -1, so the MT of the B-phase begin with 0.

model: A string or a chain of (named) strings each depicting one regression model. This is a formula expression of the standard R class. The parameters of the model are values, mt and phase.

Example

Simple example:

```
set.seed(1000)
dat \leftarrow rSC(1, d.slope = 0.5)
Trend in A and B-Phase
N persons = 1
          Intercept
                      B Beta
Linear.AB 26.702 4.544 0.970
Linear.A
            42.625 0.407 0.179
Linear.B
            47.368 5.319 0.976
Squared.AB 43.811 0.213 0.984
Squared.A 43.674 0.016 0.042
Squared.B
            60.055 0.363 0.967
Note. Measurement-times of the B-Phase start at 0
```

Advanced example:

In addition to the linear and squared regression model, two further models are computed: a) a cubic model, and b) the values predicted by the natural logarithm of the measurement time. Additionally, the data of eight single-cases are aggregated.

```
set.seed(1000)
dat \leftarrow rSC(8, d.slope = 0.3)
trendSC(dat, B.offset = 0, model = c("Cubic" = "values ~ I(mt^3)", "Log Time" =
"values ~ log(mt)"))
Trend in A and B-Phase
N persons = 8
Data of cases are aggregated using the makesingleSC command.
          Intercept
                        B Beta
           -10.139 2.723 0.945
Linear.AB
             -1.625 0.542 0.162
Linear.A
             -0.616 3.153 0.941
Linear.B
Squared.AB
              0.253 0.127 0.952
Squared.A
Squared.B
            -0.970 0.088 0.161
             9.053 0.188 0.924
Cubic.AB
              4.613 0.006 0.922
Cubic.A
Cubic.B
             -0.718 0.016 0.154
             12.948 0.012 0.884
Log Time.AB -18.201 17.317 0.825
Log Time.A
              -1.211 1.265 0.152
              -6.372 16.656 0.870
Log Time.B
```

Piecewise linear model

Note. Measurement-times of the B-Phase start at 1

Description

The plm function computes a piecewise regression model (see Huitema & Mckean, 2000). A piecewise regression models a linear trend in the data, a level and a slope increase with the start of the intervention. Additionally, the plm function computes two effect-sizes by comparing restricted to full regression models (see Beretvas & Chung, 2008). Furthermore, an autoregression model can be

used to take into account autocorrelated data (Beretvas & Chung, 2008). For the latter, your R system must comprise an installation of the nlme package.

If your dataset contains multiple single-cases, plm internally standardizes all cases and puts the data into on new single-case (see the makesingleSC command). This new case is then used to compute a piecewise regression model.

Example

Simple example:

```
set.seed(1000)
dat <- rSC(1, MT = 30, B.start = 11, d.level = 1.0, d.slope = 0.05, trend = 0.05)
plm(dat)
Piecewise Regression Analysis
F(3, 26) = 66.41; p = 0.000; R-Square = 0.885; adjusted R-Square = 0.871
                   SE
                           t
                                 p R-Square
Intercept 44.253 3.401 13.013 0.000
          0.295 0.548 0.539 0.594
         11.779 4.021 2.930 0.007
Level
                                      0.038
          0.877 0.581 1.509 0.143
                                    0.010
Slope
Separate regressions for phases
                     Slope
       Intercept
Phase A 44.25340 0.2954611
Phase B 59.28295 1.1724064
```

More complex example:

```
set.seed(2000)
dat <- rSC(3, MT = 30, B.start = 11, d.level = 1.0, d.slope = 0.05, trend = 0.05)
plm(dat, AR = 3)
Piecewise Regression Analysis
Multiple Baseline Design for 3 cases.
Correlated residuals up to autorregressions of lag 3 are modeled
F(3, 86) = 164.00; p = 0.000; R-Square = 0.851; adjusted R-Square = 0.846
                   SE
                                 p R-Square
               В
                           t
Intercept -3.009 1.608 -1.871 0.065
Trend 0.562 0.258 2.174 0.032
                                      0.005
         11.304 1.889 5.984 0.000
Level
                                      0.040
         0.407 0.275 1.482 0.142
Slope
                                      0.002
Separate regressions for phases
        Intercept
                     Slope
Phase A -3.009112 0.5617988
Phase B 25.710711 0.9692528
```

Parameters and Arguments

data, B. start and MT: Specification of the data. Read the "Introduction and example" chapter for a description.

model: Regression model used for computation (see Huitema & Mckean, 2000). Default is model = "B&L-B". Possible values are: B&L-B, H-M, Mohr#1, Mohr#2, Manly.

AR: Autoregression modelled up to the given lag. This function is only applicable when the nlme package is installed. By default, no correlated residuals are assumed (the nlme package can be easily installed with install.packages("nlme")).

Randomization tests

Description

The function rand.test computes a randomization test for single or multiple baseline single-case datasets. The function is based on an algorithm of the R-package SCRT (Bulté & Onghena, 2009, 2012) but rewritten and extended for the use in AB designs.

Example

Parameters and arguments

data, B.start: Specification of the data. Read the "Introduction and example" chapter for a description.

stat: Statistic that is computed for randomization. Default is stat = "Mean B-A").

Table.

Arguments for the stat parameter of the rand.test function.

Argument	Result
Mean A-B	Computes the difference between the mean of A and the mean of B. This is used if
	a level decrease in the B-phase is expected.
Mean B-A	Computes the difference between the mean of B and the mean of A. This is used if
	a level increase in the B-phase is expected.
Mean A-B	Computes the absolute value between the difference of the mean of the A and B-
	Phase.
Median A-B	The same as Mean A-B but based on the median.
Median B-A	The same as Mean B-A but based on the median.
В	Computes the difference between the slope parameter of a linear regression
	model for the B and A-phase. The procedure has not yet been tested for
	practicality, so it is experimental.
Bdecrease	Complementary to the BETA argument. Computes the difference between the
	slopes of the A and the B-phase. This is useful when a decrease in the slope due to
	an intervention is expected.
B plm level	Computes piecewise regression models and takes the B factors of the level
	predictor as the critical statistic.
B plm slope	Computes piecewise regression models and takes the B factors of the slope
	predictor as the critical statistic.

number: Size of the randomization distribution. The exactness of the p-value could not exceed 1/number (i.e., number = 100 results in p-values with an exactness of one percent). Default is number = 500. For a faster processing set number = 100. For a more precise p-value set number = 1000.

complete: If TRUE, the distribution is based on a complete permutation of all possible starting combinations. This setting overwrites the number Argument. The default setting is FALSE.

limit: Minimal length of the A- und B-phase in the randomization sample. Default is limit = 5.

exclude.equal: If set FALSE, random distribution value that are equal to the observed distribution are counted as values of the distribution of the null-hypothesis. That is, they decrease the probability of rejecting the null-hypothesis (increase the p-value). Default is exclude.equal = FALSE. This should be set to TRUE if you analyse one single-case design (not a multiple baseline data set) to get a sufficient test-power but be aware it increases the chance of an alpha-error.

graph: If TRUE, a histogram of the resulting distribution is plotted. Default is HIST = FALSE.

output and data.check: Functions for speed optimization in a Monte-Carlo analysis. Defaults are output = "c" and data.check = TRUE.

Plot AB-designs

Description

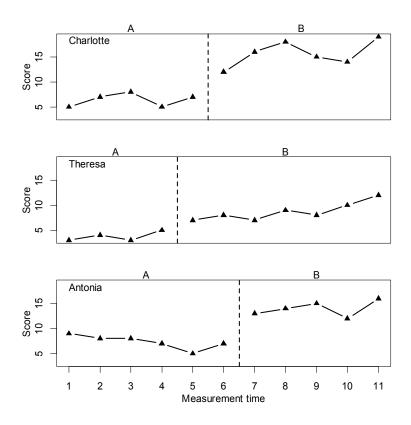
The plotsc command draws a nice plot of one or multiple single-cases. By default, plotsc draws a multiple single-case plot if the given data contains more than one case.

You can export the plot in several graphic formats including jpeg, tiff, pdf, and as a vector graphic either using the clipboard or writing it into a file. Windows users can easily use the file-menu of the plot window that comes up when drawing a plot to export the graphic.

Example

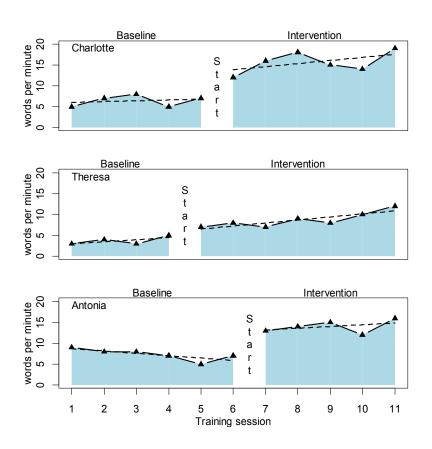
The default settings of the plotsc command using the data from the introduction chapter:

plotSC(study1)

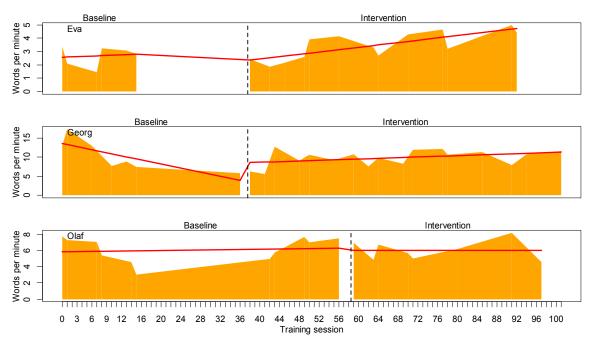


An example of a customized setup with the same data:

plotSC(study1, ylim = c(0,20), fill = "light blue", xlab = "Training session", ylab = "words per minute", text.ABlag = "Start", phase.names = c("Baseline", "Intervention"), lines = "trend")



A third example with the data of the study from Grosche (2011):



Parameters and arguments

data, B. start and MT: Specification of the data. Read the "Introduction and example" chapter for a description.

phase.names: SCDA uses the default names "A" and "B" for the two experimental phases. You can change these with the phase.names parameter. Example: phase.names = c("Baseline", "Treatment").

case.names: SCDA tries to extract the case names from the given data. If that is not possible, no case names are included in the plot. If you want to set the case names explicitly, you can use the case.names parameter. Example: case.names = c("Antonia", "Charlotte", "Theresa").

lines: Adds one or more lines or curves to the plot for a better estimation of statistical parameters. The argument is either given as a single character string lines = "median" or a chain of character strings lines = c("median", "trend"). Additionally, some of the procedures can be refined by a single argument e.g., lines = c("mean" = 0.10) adds 10% trimmed mean lines

Table: Arguments for the parameter lines.

Argument	Result
median	A median line for the A and B-phase.
mean	A mean line for the A and B-phase. Default is a 10% trimming. Other trimming values can be set by a second parameter e.g., lines = c(mean = 0.2) draws a 20% trimmed mean line.
trend	A trend line for the A and B-phase.
trendA	A trend line for the A-phase.
maxA Or pnd	A line for the maximum of the A-phase.
medianA	A line for the median of the A-phase.
meanA	A line for the 10% trimmed mean of the A-phase. Trimming can be changed in the following way lines = c(meanA = 0.15).
plm or piecewisereg	A regression line for a piecewise linear regression model.
plm.ar	A regression line for a piecewise autoregression model. The lag is specified by plm.ar = 2. Where the number is the maximum order of the autoregression analysis.
movingMean	Draws a moving mean curve. The lag can be specified by lines = c(movingMean = 2). Default is a lag 1 curve.
movingMedian	Draws a moving median curve. The lag can be specified by lines = c(movingMedian = 3). Default is a lag 1 curve.
loreg	A non-parametric local regression line. The proportion of data influencing each data point can be specified by lines = c(loreg = 0.66). The default is 0.5.
lty, lwd, col	Specifies line type ltw, line width lwd, and line colour col. Default is a black dashed line with the width 2. E.g., to draw a solid red thick mean line type lines = c(mean, lty = "solid", lwd = 4, col = "red"). Some of the

possible line types are "solid", "dashed",	and
"dotted".	

fill.col: If set, the area beneath the plot line is coloured in the given colour (e.g., fill.col = "grey"). Use the standard R command colours() to get a list of possible colours.

textAB.lag: By default, SCDA draws a vertical line to separate the A and B-phase. Alternatively, you could print a character string between the two phases using the textAB.lag parameter (e.g., textAB.lag = "Start").

Some standard parameters of the R plot function that are useful here:

xlim and ylim: Lower and upper limit for the x- and y-axis of the plot (e.g., ylim = c(0, 20) sets the y-axis to a scale from 0 to 20). In multiple single cases plots you can use ylim = c(0, NA) to scales the y-axis from 0 to the maximum of each case. If the xlim and ylim parameter is not set, SCDA automatically computers a proper scale.

xlab and ylab: Set the labels for the x and y-axis. The defaults are "Measurement time" and "Score" (e.g., xlab = "Sessions").

type: Sets the plot type. "I" draws lines, "p" points, "b" draws lines and points, and "n" draws nothing onto the plot (default of plotSC is "b"). The "n" argument can be useful in combination with the lines argument (e.g., type = "n", lines = "loreg").

1wd: Width of the plot lines. Default is 2.

pch: Point type. Default is 17. (e.g., pch = 16 draws filled circles; pch = "A" draws As).

Figure: Some possible values for the pch parameter of the plotsc function.

Smoothing

Description

This command provides three different procedures to smooth the data (i.e., to eliminate noise).

A moving average function (either mean based or median based) replaces step-by-step each data point by the average of the surrounding data. With a local regression function, each data point is regressed by its surrounding values.

Example

Parameters and Arguments

data, B. start and MT: Specification of the data. Read the "Introduction and example" chapter for a description.

FUN: Function to compute the smoothing. Default is a lag 1 moving Median function.

Table: Arguments for the parameter FUN.

Argument	Result
movingMean	Computes the moving mean.
movingMedian	Computes the moving median.
localRegression	Computes non-parametric local regressions.

intensity: In the case of movingMean or movingMedian it is the lag (i.e., the range of values around the target value) that is used for computing the average (default is 1). In case of localRegression it is the proportion of data influencing each data point (default is 0.2).

Outlier

Description

Identifies and drops outliers for each case of your data file. The function returns a new data file without the outlier data. Criteria for outlier identification can be standard deviations, confidence intervals, and Cook's distance (based on a piecewise linear regression model).

Example

To "clean" the original data from Grosche (2011) without the outliers and using Cook's distance greater 4/n as a criteria, type:

```
new.data <- outlierSC(Grosche2011SC, criteria = c("Cook", "4/n"))
Outlier analysis for single case data
Criteria: Cook's distance based on piecewise regression exceeds 4/n
Eva : Dropped 1 data
Georg : Dropped 3 data
Olaf : Dropped 2 data</pre>
```

The object new.data contains the "cleaned" data and can be used now for further analyses (e.g., describeSC(new.data)).

Parameters and Arguments

data, B. start and MT: Specification of the data. Read the "Introduction and example" chapter for a description.

criteria: Specifies criteria for dropping data. Default is criteria = c("SD", 2) i.e, drop all values exceeding two standard deviations.

Table: Arguments for the parameter crtieria.

Argument	Result
SD	Standard deviations.
CI	Confidence interval. 0.95 represents a 95% confidence interval.

Cook's distance based on the piecewise-linear-regression model. To exclude cases where cook exceeds 4/n set:
criteria = c("Cook", "4/n").

Fill in missing measurement times

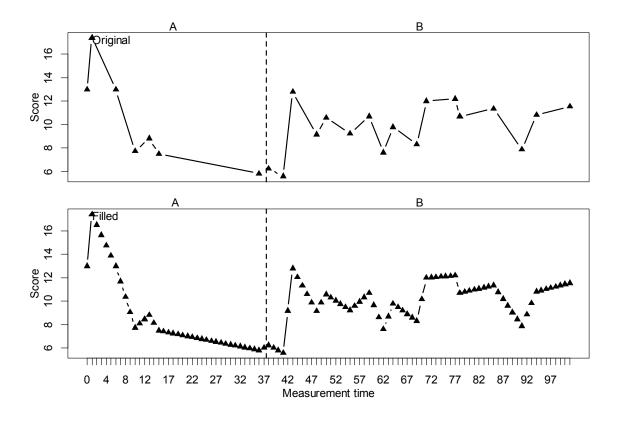
Description

The command fillmissingSC() fills in missing measurements if a single-case or multiple single-cases by interpolation.

Example

In the study of Grosche (2011) measurements couldn't be realized each single week for all participants. During the course of 100 weeks, about 20 measurements per person at different times were administered. Here is a way to fill in the missing data:

```
new.data <- fillmissingSC(Grosche2011SC)
plotSC(list(Original = Grosche2011SC[[2]], Filled = new.data[[2]]))</pre>
```



Parameters and Arguments

 \mathtt{data} , $\mathtt{B.start}$ and \mathtt{MT} : Specification of the data. Read the "Introduction and example" chapter for a description.

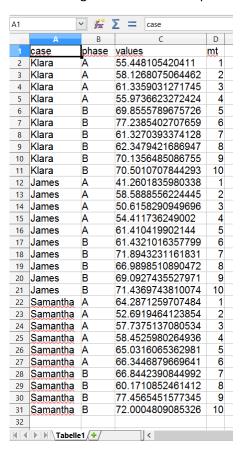
Importing and exporting data

Description

If you want to export or import your data for the use with other programs (like EXCEL or CALC) you can use the readsc and writesc commands.

Example

The resulting data file can be imported into a spreadsheet program and looks something like this:



Vice versa, a data file of the given structure can be exported as a CSV file and then be imported with

```
dat <- readSC("example.csv")</pre>
describeSC(dat)
Describe single-case data
           James
                   Klara Samantha total
n A
            5.00
                   4.000
                             6.00 15.00
n B
            5.00
                   6.000
                             4.00 15.00
                             60.76 57.25
           53.26 57.721
Mean A
                            69.12 68.62
           68.17 68.568
Mean B
Mean dif
           14.91 10.847
                             8.36 11.37
            7.86
SD A
                   2.674
                             5.32
                                   5.69
SD B
            4.25
                   5.902
                             7.37
                                   5.98
```

7.287

7.24 8.22

9.86

SD AB

```
1.90 4.056 1.57 2.51
SMD A
SMD B
        3.51 1.838
                      1.13 2.16
SMD AB
        1.51 1.488
                      1.15 1.38
Autocor A -0.29 -0.269
                      0.12 -0.15
Autocor B -0.38 -0.076 -0.19 -0.21
Trend A 3.61 0.479
                      1.37 1.82
        1.72 -0.487
Trend B
                      3.28 1.50
Trend AB 2.91 1.503
                      1.71 2.04
PND 100.00 83.333
                      75.00 86.11
      100.00 100.000 75.00 91.67
PEM
NAP
       100.00 95.833 87.50 94.44
        100.00 80.000
PAND
                      80.00 86.67
```

Note that most windows systems in Germany are set up with a "i" as a separator and a "," as a decimal sign. If you have a system like this, you can use the sep = "i", dec = ", " parameters in the writesc and readsc command to specify this condition.

Parameters and Arguments

dat: Data file to be exported (only for the writesc command)

filename: Name of the file to be exported or imported

sort.labels: If set TRUE resulting list is sorted by label names (alphabetically, increasing). Default is FALSE.

sep: Variable separator (default is ",")

dec: Decimal sign (default is ".")

Selecting data

Description

If you want to select a certain subset of the data, you can use the selectSCData command.

Example

The example dataset by Heartsc contains single-case data of students learning vocabulary by heart in 20 sessions with additional five pre-training measurements.

If you want to plot the first to the 20th measurement type:

```
newData <- selectSCData(byHeartSC, select = 1:20)
plotSC(newData)</pre>
```

Parameters and Arguments

Random sample generator

Description

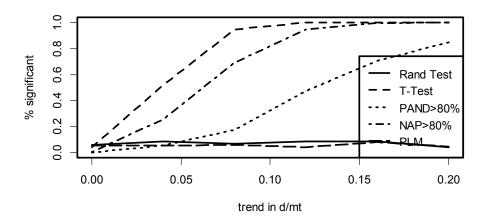
SCDA offers a module for generating random single- and multiple-baseline samples.

Example

```
set.seed(1234)
study <- rSC(3, d.level = 0.7, d.slope = 0.1, concise = TRUE)
plm(study, AR = 2)
Piecewise Regression Analysis
Multiple Baseline Design for 3 cases.
Correlated residuals up to autorregressions of lag 2 are modeled
F(3, 56) = 63.43; p = 0.000; R-Square = 0.773
                               p R-Square
              В
                  SE
                          t
Intercept 0.117 0.328 0.357 0.723
         Level
                                    0.018
          0.178 0.100 1.776 0.081
Slope
                                    0.015
```

As a more advanced example, that requires some knowledge in R-programing see the following Monte-Carlo study on the influence of trends on the power of different analysing techniques.

```
op <- par(lwd = 3, mfrow = c(2,1))
for(d in c(0,1)){
 it <- seq(0, 0.2, length = 6)
 study <- list()</pre>
 for(i in 1:length(it))
    study[[i]] <- rSC(n = 150, MT = 20, B.start = 10, d.level = d, trend = it[i],
rtt = 0.8, concise = TRUE)
 p.rand <- lapply(study, function(x) unlist(lapply(x, function(x)</pre>
rand.test(list(x), number = 100, output = "p", exclude.equal = TRUE,data.check =
FALSE))))
 p.t <- lapply(study, function(z) unlist(lapply(z, function(y) t.test(values~phase,</pre>
data = y, alternative = "less", var.equal = TRUE)$p.value)))
 p.pand <- lapply(study, function(z) unlist(lapply(z, function(y) pand(y)$PAND)))</pre>
 = FALSE)[[1]])))
 p.plm <- lapply(study, function(z) unlist(lapply(z, plm.mt)))</pre>
 y \leftarrow unlist(lapply(p.rand,function(x) mean(x<=0.05)))
 plot(it, y, xlab = "trend in d/mt", ylab = "% significant", type = "l", ylim =
c(0,1))
 y <- unlist(lapply(p.t,function(x) mean(x<=0.05)))</pre>
 lines(it,y, lty = 2)
 y <- unlist(lapply(p.pand,function(x) mean(x>80)))
 lines(it,y, lty = 3)
 y <- unlist(lapply(p.nap,function(x) mean(x>80)))
 lines(it,y, lty = 4)
 y \leftarrow unlist(lapply(p.plm,function(x) mean(x<=0.05)))
 lines(it,y, lty = 5)
 legend("bottomright", legend = c("Rand Test", "T-Test", "PAND>80%", "NAP>80%",
"PLM"), lty = 1:5)
par(op)
```



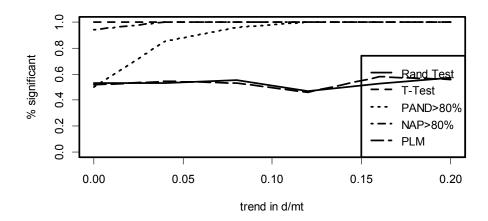


Figure. Alpha-error (upper plot) and testpower (lower plot) of different statistical techniques for analysing single-case data with an increasing trend.

Parameters and Arguments

n: Number of studies to be created (default is n = 1).

MT: Measurement times of single cases in each study (default MT = 20).

B.start: Starting values of the B-phase. A single value (e.g., B.start = 6) defines the B.start for all studies and cases. A vector of starting values is given with the chain command (e.g., B.start = c(6, 7, 8)). A value between 0 and 1 is interpreted as a proportion (e.g., B.start = c(0.3, 0.5, 0.8) are starting point at 30%, 50% and 80% of the length defined in MT). For randomized starting point, you can use B.start = c("rand", 5, 10) which computes random values for each study with values between 5 and 10 or B.start = c("rand", 0.25, 0.75) which computes random starting points between 25% and 75% of the length defined in MT.

cases: Number of cases per study. E.g., n = 10, cases = 3, B.start = c(7,9,11) creates 10 multiple-baseline designs with 3 persons (Starting point of the B-phase at 7, 9, 11, respectively) each.

trend: Defines a trend in d per measurement across all measurements. E.g., trend = 0.1 is an increase of 0.1 standard deviations per measurement.

m and s: Mean and standard deviation of the sample distribution the data are drawn from.

d.level: A single level increase with the beginning of the B-Phase in standard deviations.

d.slope: Amount of increase in standard deviations per measurement time starting with the Beginning of the B-phase (e.g., d.slope = 0.1 generates an incremental increase of 0.1 standard deviations for each measurement of the B-phase).

rtt: Reliability of the underlying simulated measurements (default is rtt = 0.8).

concise: If set TRUE, no information about the generated sample is given (default is FALSE).

check: If set TRUE, the generated samples mean, sd, and rtt is analysed (default is FALSE).

round: Rounds the measurement values to a specific decimal position (e.g., round = 2).

extreme.p: Probability of extreme values (e.g., extreme.p = 0.05 gives a 5% probability of an extreme value; default = 0).

extreme.d: Range of an extreme value in d (e.g., extreme.d = c(-7, -6) results in extreme values within a range of -7 and -6 standard deviations). Default is c(-4, -3). Caution: the first value must be smaller than the second, otherwise the procedure will fail.

random.names: Just a gimmick. If set TRUE cases have random first names. The selection of names is drawn from a list of the 2000 most popular names for births in the U.S.A. 2012 (1000 names for boys and 1000 names for girls). Default is FALSE.

Aggregate multiple cases into one case

Description

The makesinglesc command combines multiple single cases into one single case which can be used for further analysis.

The algorithm works the following way:

- All measurements of each single-case are mean-centred with respect to the mean of the Aphase of each single-case.
- 2) The values of the A-phases of all single-cases are combined and ordered ascending with respect to the measurement times.
- 3) The values of the B-phases are combined and ordered as well.
- 4) The measurements of the B-phases are attached behind the A-phase measurements. The measurement times of the B-phase are shifted to start one measurement time after the Aphase.

Parameters and Arguments

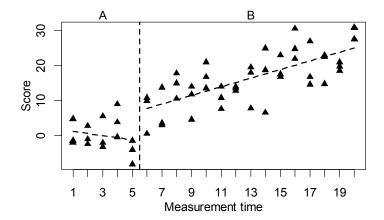
data, B. start and MT: Specification of the data. Read the "Introduction and example" chapter for a description.

scale: If set TRUE, values are standardized to the deviation of the A-phase. Default is FALSE.

type: By default values with the same measurement-time are added. If type is set to mean or median, values of the same MT are replaced with their mean or median. Default is add.

Example

```
study1 <- rSC(3, d.level = 0.8, d.slope = 0.1, round = 0)
new.sc <- makesingleSC(study1)
plotSC(new.sc, type = "p", lines = "trend")</pre>
```



*(Experimental) Power Analysis

Description

The power.testsc command conducts a Monte-Carlo study on the test-power and alpha-error of a randomization-test and a piecewise-regression model. The distribution values of the Monte-Carlo sample is either defined or automatically estimated based on the data of an actual study.

Parameters and Arguments

n: Size of Monte-Carlo study (default is n = 100).

MT: Measurement times of single cases random study (default MT = 20).

B.start: Starting values of the B-phase. A single value (e.g., B.start = 6) defines the B.start for all studies and cases. A vector of starting values is given with the chain command (e.g., B.start = c(6, 7, 8)). A value between 0 and 1 is interpreted as a proportion (e.g., B.start = c(0.3, 0.5, 0.8) are starting point at 30%, 50% and 80% of the length defined in MT). For randomized starting point, you can use B.start = c("rand", 5, 10) which computes random values for each study with values between 5 and 10 or B.start = c("rand", 0.25, 0.75) which computes random starting points between 25% and 75% of the length defined in MT.

cases: Number of cases per study. E.g., n = 10, cases = 3, B.start = c(7,9,11) creates 10 multiple-baseline designs with 3 persons (Starting point of the B-phase at 7, 9, 11, respectively) each.

trend: Defines a trend in d per measurement across all measurements. E.g., trend = 0.1 is an increase of 0.1 standard deviations per measurement.

 \mathfrak{m} and \mathfrak{s} : Mean and standard deviation of the sample distribution the data are drawn from.

d.level: A single level increase with the beginning of the B-Phase in standard deviations.

d.slope: Amount of increase in standard deviations per measurement time starting with the Beginning of the B-phase (e.g., d.slope = 0.1 generates an incremental increase of 0.1 standard deviations for each measurement of the B-phase).

rtt: Reliability of the underlying simulated measurements (default is rtt = 0.8).

extreme.p: Probability of extreme values (e.g., extreme.p = 0.05 gives a 5% probability of an extreme value; default = 0).

extreme.d: Range of an extreme value in d (e.g., extreme.d = c(-7, -6) results in extreme values within a range of -7 and -6 standard deviations). Default is c(-4, -3). Caution: the first value must be smaller than the second, otherwise the procedure will fail.

limit: Minimal length of the A- und B-phase in the randomization sample. Default is limit = 5.

exclude.equal: If set FALSE, random distribution value that are equal to the observed distribution are counted as values of the distribution of the null-hypothesis. That is, they decrease the probability of rejecting the null-hypothesis (increase the p-value). Default is exclude.equal = "auto" (FALSE for multiple-baseline designs and TRUE for single baseline designs).

alpha: Alpha level used to calculate the proportion of significant tests. Default is 0.05.

stat: Defines the statistics the power analysis is computed for. The default stat = c("rand.test", "plm") computes a power-analysis for the randomization and the plm analysis.

rand.test.stat: Defines the statistic a randomization test is based on. The first values stipulates the statistic for the level-effect computation and the second value for the slope-effect computation.

Deafult is rand.test.stat = c("Mean B-A", "B").

Example

> power.testSC(fillmissingSC(Grosche2011SC))
Compute Monte-Carlo power-analyses with the following parameters:

```
Sample studies
                100
Cases per sample 3
               5.537086
M
SD
               3.039698
MT
               93
B.start
               39 39 60
               0.8
rtt
d level
               0.3274
d slope
               0.0197
d trend
                -0.0079
Extreme.p
                -4 -3
Extreme.d
Alpha level
               0.05
Exclude equal
               FALSE
Limit
```

Test-Power in percent:

			Power	Alpha-error
Rand-Test:	Mean	B-A	12	0
Rand-Test:	В		0	1
PLM: Level			85	4
PLM: Slope			100	6

Reference

- Beretvas, S., & Chung, H. (2008). An evaluation of modified R²-change effect size indices for single-subject experimental designs. *Evidence-Based Communication Assessment and Intervention*, 2, 120–128.
- Bulté, I., & Onghena, P. (2009). Randomization tests for multiple-baseline designs: An extension of the SCRT-R package. *Behavior Research Methods*, *41*(2), 477–485. doi:10.3758/BRM.41.2.477
- Bulté, I., & Onghena, P. (2012). SCRT: Single-Case Randomization Tests. Abgerufen von http://cran.r-project.org/web/packages/SCRT/index.html
- Grosche, M. (2011). Effekte einer direkt-instruktiven Förderung der Lesegenauigkeit. *Empirische Sonderpädagogik*, 3(2), 147–161.
- Huitema, B. E., & Mckean, J. W. (2000). Design specification issues in time-series intervention models. *Educational and Psychological Measurement*, *60*(1), 38–58.
- Parker, R. I., Hagan-Burke, S., & Vannest, K. (2007). Percentage of All Non-Overlapping Data (PAND)

 An Alternative to PND. *The Journal of Special Education*, 40(4), 194–204.
- Parker, R. I., & Vannest, K. (2009). An improved effect size for single-case research: Nonoverlap of all pairs. *Behavior Therapy*, *40*(4), 357–367.
- Wise, E. A. (2004). Methods for analyzing psychotherapy outcomes: A review of clinical significance, reliable change, and recommendations for future directions. *Journal of Personality***Assessment, 82(1), 50–59.